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## hp calculators

HP 33S Applications in mechanical engineering

Applications in mechanical engineering
Practice solving problems in mechanical engineering

- Application 1: Stress on an element (Mohr circle)
- Application 2: Gear forces (worm gears)



## Applications in mechanical engineering

This training aid will illustrate the application of the HP 33S calculator to several problems arising in mechanical engineering. These examples are far from exhaustive, but do indicate the incredible flexibility of the HP 33S calculator.

## Practice solving problems in mechanical engineering

## Application 1: Stress on an element (Mohr circle)

The Mohr circle equations convert an arbitrary stress configuration to principal stresses, maximum shear stress, and rotation angle. It is then possible to calculate the state of stress for an arbitrary orientation $\theta^{\prime}$.


Figure 1
The Mohr circle formulas are shown below, where $s$ is the normal stress, $\tau$ is the shear stress, $s_{x}$ is the stress in the $x$ direction for Mohr circle input, $s_{y}$ is the stress in the $y$ direction for Mohr circle input, $\tau_{\mathrm{xy}}$ is the shear stress on the element for the Mohr circle input, $s_{1}$ and $s_{2}$ are the principal stresses, $\theta$ is the rotation angle, and $\tau_{\max }$ is the maximum shear stress. Note that $\theta$ is the angle of rotation from the specified axis to the principal axis, and so should be thought of as a negative angle. This is opposite to the normal Mohr circle convention.

$$
\begin{array}{lll}
\text { Maximum shear stress } & \tau_{\max }=\sqrt{\left(\frac{\mathrm{s}_{\mathrm{x}}-\mathrm{s}_{\mathrm{y}}}{2}\right)^{2}+\tau_{\mathrm{xy}}^{2}} & \text { Figure 2 } \\
\text { Principal stress } & \mathrm{s}_{1}=\frac{\mathrm{s}_{\mathrm{x}}+\mathrm{s}_{\mathrm{y}}}{2}+\tau_{\max } & \text { Figure 3 } \\
\text { Principal stress } & \mathrm{s}_{2}=\frac{\mathrm{s}_{\mathrm{x}}+\mathrm{s}_{\mathrm{y}}}{2}-\tau_{\max } & \text { Figure 4 } \\
\text { Rotation angle } & \theta=\frac{1}{2} \tan ^{-1}\left(\frac{2 \tau_{\mathrm{xy}}}{\mathrm{~s}_{\mathrm{x}}-\mathrm{s}_{\mathrm{y}}}\right) & \text { Figure 5 }
\end{array}
$$

Example: If $s_{x}=25,000 \mathrm{psi}, \mathrm{s}_{\mathrm{y}}=-5,000 \mathrm{psi}$, and $\mathrm{T}_{\mathrm{xy}}=4,000 \mathrm{psi}$, compute the principal stresses, the angle of rotation $\theta$, and the maximum shear stress.

Solution: $\quad$ Solve for the maximum shear stress, $\tau_{\text {max }}$.
 $\pm \sqrt{x}$ STO $T$

In algebraic mode: $2 \mathbf{2} 500000-500000$ $\pm 400000 x^{2}$ ENTER $\sqrt{x}$ STO $T$

```
5241,000,000
15.524.1747
```

Solve for the principal stress, $\mathrm{s}_{1}$.
In RPN mode: 2050000 ENTER 50000
In algebraic mode: $250000 \times 50000 \pm$ ENTER $\div 2+2$

## $20000 \div 2+T=$ <br> 25.524 .1747

Solve for the principal stress, $s_{2}$.




Solve for the rotation angle, $\theta$.
 $\square \square$ ATAN 2 -


ATAN2.666666666 7.4657

Figure 9
Answer: The principal stresses, $\mathrm{s}_{1}$ and $\mathrm{s}_{2}$, are 25,524 psi and $-5,524$ psi. The angle of rotation, $\theta$, is 7.4657 degrees. The maximum shear stress is 15,524 psi.

## Application 2: Gear forces (worm gears)

There are three mutually perpendicular forces resulting from input torque on worm gears as shown below.


Figure 10
The worm gear force formulas are shown below, where T is the input (worm) torque, n is the pitch radius of the worm, $F_{t}$ is the tangential force on the worm, $\alpha$ is the lead angle of the worm, $L$ is the lead of the worm, $r$ is the pitch radius of the worm gear, $\phi_{n}$ is the pressure angle measured perpendicular to the worm teeth, $\phi$ is the pressure angle measured parallel to the worm axis, $f$ is the coefficient of friction, $F_{w s}$ is the separating force between the worm and the gear, and $\mathrm{F}_{\text {gax }}$ is the force parallel to the gear axis.

Tangential force

$$
\begin{equation*}
F_{t}=\frac{T}{r} \tag{Figure 11}
\end{equation*}
$$

Separating force - worm and gear $\quad \mathrm{F}_{\mathrm{ws}}=\mathrm{F}_{\mathrm{t}}\left(\frac{\sin \phi_{\mathrm{n}}}{\cos \phi_{\mathrm{n}} \sin \alpha+\mathrm{f} \cos \alpha}\right) \quad$ Figure 12
Force parallel to gear axis $\quad \mathrm{F}_{\mathrm{gax}}=\mathrm{F}_{\mathrm{t}}\left(\frac{1-\frac{\mathrm{f} \tan \alpha}{\cos \phi_{\mathrm{n}}}}{\tan \alpha+\frac{\mathrm{f}}{\cos \phi_{\mathrm{n}}}}\right) \quad$ Figure 13

Lead angle
$\alpha=\tan ^{-1}\left(\frac{\mathrm{~L}}{2 \pi \mathrm{r}}\right)$
Figure 14

Pressure angle parallel to worm gear

$$
\phi=\tan ^{-1}\left(\frac{\tan \phi_{\mathrm{n}}}{\cos \alpha}\right)
$$

Example: A torque of $512 \mathrm{in}-\mathrm{lb}$ is applied to a worm gear having a pitch diameter of 2.92 inches and a lead of 2.2. inches. The normal pressure angle is 20 degrees and the coefficient of friction is 0.10 . Find the lead angle, the forces on the worm and worm gear, and the tangential force.

Solution: $\quad$ Solve for tangential force and store it in variable F.



Figure 16
Solve for the lead angle and store it in variable A. Make sure the HP 33S is in degrees mode first.
In RPN mode

```
MODES 1
```



```
(4) ATAN STO A
```

In algebraic mode: MODES 1
$2 \cdot 2 \div 2 \div \square$



Solve for the separating force on the worm.






Solve for the force parallel to the gear axis.
 $0 \cdot 1$ ENTER 20 COS $\div$ RCL AITAN $+\div$ RCL $\mathrm{F}^{\boldsymbol{x}} \times$

 20 COS RODEDTER

Answer: The lead angle is 13.49 degrees, the separating force on the worm is approximately 379 pounds and the force parallel to the worm gear axis is approximately 987 pounds. The tangential force is approximately 351 pounds.

